Two-Sided Matching via Balanced Exchange

Umut Mert Dur^\dagger M. Utku Ünver ‡



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1 Introduction

We introduce and model a new class of two-sided matching markets without explicit transfers, in which there is an additional fundamental constraint.¹ The eventual market outcome is linked to an initial status-quo matching, which may give participants certain rights that constrain how future activity can play out. Since market outcome is typically di erent from the status quo, such activities loosely resemble an exchange in which one side of the agents are changing or acquiring new partners in addition to the two-sided matching market structure. In such markets, a fundamental balancedness condition needs to be sustained with respect to the status-quo matching. The motivation for such a balancedness constraint can be di erent depending on the features of the market. Two contrasting examples are labor and higher education markets, where workers and colleges provide services to be compensated, respectively. In worker exchange, a worker needs to be replaced with a new one at her home firm so that this firm can function properly, and thus, the market needs to clear in a balanced manner. In student exchange, the college that is matched with an exchange student should be able to send out a student as well so that its education costs do not increase, and thus, the market needs to clear in a balanced manner. There are several prominent examples of such exchanges, such as national and international teacher-exchange programs, clinical-exchange programs for medical doctors, worker-exchange programs within or across firms, and student-exchange programs among colleges. This balancedness constraint induces preferences for firms/colleges not only over whom they get matched with (i.e., import), but also over whom they send out (i.e., export). The most basic kind of such preferences requires the firm/college to have a preference for balanced matchings, i.e., for import and export numbers to be equal. We analyze our model over two explicit market applications: (permanent) tuition exchange and temporary worker exchange (see Section 2 for details).

In tuition exchange

their preferences over matchings are determined through their rankings over the incoming class and how balanced the eventual matching is.² We start by showing, through a simple example, that individual rationality and nonwastefulness, standard concepts in two-sided matching markets, and balancedness are in general conflicting requirements (Proposition 1). For this reason, we restrict our attention to the set of balanced-e cient mechanisms. Unfortunately, there exists no balanced-e cient and individually rational mechanism that is immune to preference manipulation for colleges (Theorem 2).

Although 2S-TTC is balanced-e cient, it may not match the maximum possible number of students while maintaining balance. We show that if the maximal-balanced solution is di erent from the 2S-TTC outcome for some preference profile, it can be manipulated Compared to deferred-acceptance-based current practice, they show that a TTC-based approach doubles the number of teachers moving from their initial assignment. Additionally, when the distribution of the ranks of teachers over the schools are considered, the outcome of the TTC-based approach stochastically dominates that of the current practice. Thus, there exist real-life settings, in which our proposals can lead to significant welfare improvements.

We extend this model for temporary worker exchanges, such as teacher-exchange programs. We tweak our model slightly and assume that the quotas of the firms are fixed at the number of their current employees, and, hence, firms would like to replace each agent who leaves. We also assume that firm preferences are coarser than colleges in tuition exchange due to the temporary nature of the exchanges. We assume they have weakly size-monotonic preferences over workers: larger groups of acceptable workers are weakly better than weakly smaller groups of acceptable workers when the balance of the matching with larger groups of acceptable workers is zero and the balance of the matching with smaller group of worker is nonpositive.⁹ Many colleges give qualified dependents of faculty tuition waivers. Through a tuitionexchange program, they can use these waivers at other colleges and attend these colleges for free. The dependent must be admitted to the other college

rent form.¹⁸ The Jesuit universities exchange program FACHEX is another one that is adversely a ected. The program still does not have an explicitly embedded balancedness requirement. It includes all Jesuit universities but Georg

students by c. Let $_{C}$ = ($_{c})_{c}$ $_{C}$ be the list of college ${\bf internal \ priority \ orders}$ where $_{c}$ is a linear order over S_{c}

In a revelation game, students and colleges report their preferences; additionally, colleges report their admission and eligibility quotas.²⁶ A mechanism is immune to preference manipulation for students or colleges if for all $[q, e, \succeq]$, there ex-S (or i C) and \succeq_i such that $[q, e, (\succeq_i, \succeq_{-i})](i)$ i $[q, e, \succeq_i](i)$. A ists no i is immune to preference manipulation if it is immune to preference mechanism manipulation for both students and colleges. A mechanism is immune to quota **manipulation** if for all $[q, e, \succeq]$, there exists no c C and (q_c, e_c) with q_c q_c such that $[(q_c, q_{-c}), (e_c, e_{-c}), \succeq](c) \ c \ [q, e, \succeq](c)$. A mechanism is strategy proof for colleges if for all $[q, e, \succeq]$, there exists no c C and (q_c, e_c, \succeq_c) with q_c q_c such that $[(q_c, q_{-c}), (e_c, e_{-c}), (\succeq_c, \succeq_{-c})](c) \quad c \quad [q, e, \succeq](c)$. A mechanism is strategy proof for students if it is immune to preference manipulation for students. A mechanism is strategy proof if it is strategy-proof for both colleges and students.²⁷ A mechanism

is group strategy proof for students if for all [q, e, \succsim], there exists no S $\,$ S and

Throughout our analysis, we impose a weak restriction on college preferences. Assumption 1 below states that a college prefers a better scholarship class with zero net balance to an inferior scholarship class with a nonpositive net balance.

 $\label{eq:assumption} {\bf Assumption} \quad \mbox{For any } \mu, \qquad \mbox{M^u and c} \quad \mbox{C, if $b^\mu_c=0$, b_c} \quad \ 0$, and $\mu(c) P^c$}$

2017). In contrast, in our market, college slots are not objects. Therefore our definition of a mechanism, and the properties of matchings and mechanisms (except strategy-proofness for students) do not have any analogous translation in such problems. However, because

Theorem Under Assumption 1 and when true eligibility quotas satisfy $e_c = |S_c|$ for all c C, 2S-TTC is immune to quota manipulation.

We prove the theorem with a lemma showing that as the quotas of a college increase, the import and export sets and the admitted class of students of this college also (weakly) expand under 2S-TTC.³²

Theorems 3 and 4 point out that only colleges can benefit from manipulation, and they can manipulate by misreporting their preferences. Moreover, the only way to manipulate preferences is to report an acceptable student as unacceptable. Suppose we take all the admitted students in the regular admission procedure as acceptable for a tuition-exchange scholarship. Then, to manipulate 2S-TTC, a college needs to reject a student who satisfies the college admission requirements. Usually college admission decisions are made before the applicants are considered for scholarships.³³

Proposition 2 below implies that colleges do not benefit from misreporting their ranking over incoming classes.

Proposition Under Assumption 1, colleges are indi erent among strategies that report preferences in which the same set of students is acceptable with the same quota report under the 2S-TTC mechanism.

We have shown that 2S-TTC has appealing properties. In the following theorem, we show that it is the unique mechanism satisfying a subset of these properties.

Theorem 5 Under Assumption 1, 2S-TTC is the unique student-strategy-proof, acceptable, and balanced-e cient mechanism that also respects internal priorities.

In the proof of our characterization theorem, we use a di erent technique from what is usually employed in elegant single quota characterization proofs such as Svensson (1999) and Sönmez (1995) for the result of Ma (1994). Our proof relies on building a contradiction with the claim that another mechanism with the four properties in the theorem's

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hypothesis can exist. Suppose such a mechanism exists and finds a di erent matching than 2S-TTC for some market. The 2S-TTC algorithm runs in rounds in which trading cycles are constructed and removed. Suppose S(k) is the set of students removed in Round k, while running 2S-TTC in such a way that in each round only one arbitrarily chosen cycle is removed and all other cycles are kept intact. We find a Round k and construct an auxiliary market with the following three properties: (1) Eligibility quotas of home colleges of students in S(k) are set such that these are the last certified students in their respective home institutions; (2) all preferences are kept intact except those of students in S(k) are assigned c under the alternative mechanism, while all students removed in the 2S-TTC algorithm before Round k have the same assignment under 2S-TTC and the alternative mechanism. This contradicts the balanced-e ciency of the alternative mechanism: we could give the students in S(k) their 2S-TTC assignments while keeping all other assignments intact and obtain a Pareto-dominating balanced matching. Round k and the auxiliary market are constructed in three iterative steps.

Among all the axioms, only the respect for internal priorities is based on exogenous rules. One might suspect that more students will benefit from the tuition-exchange program if we allow the violation of respect for internal priorities. However, such mechanisms turn out to be manipulable by students.

Theorem 6 Any balanced and individually rational mechanism that does not assign fewer students than 2S-TTC and selects a matching in which more students are assigned whenever such a balanced and individually rational outcome exists, is not strategy-proof for students, even under Assumption 1.

4.1 Market Implementation: Tuition Remission and Exchange Incorporating tuition-remission I29552(s(t07Tc1nc)50(e)50(d)c)2gT u50(d)bp50(d)piooo

in a semi-decentralized fashion: first, colleges announce their tuition-exchange scholarship quotas and which of their students are eligible to be sponsored for both exchange and remission; then, eligible students apply for scholarship to the colleges they find acceptable; then colleges send out scholarship admission letters. At this stage, as students have also learned their opportunities in the parallel-running regular college admissions market, they can form better opinions about the relative ranking of the null college, i.e., their options outside the tuition-exchange market. Students submit rankings over the colleges that admitted them with a tuition-exchange scholarship and the relative ranking of their outside option. Finally, 2S-TTC is run centrally to determine the final allocation.

4.2 Allowing Tolerable Imbalances

Some programs care about approximate balance over a moving time window. Here, we relax the zero-balance constraint and allow each c C to maintain a balance within an interval $[_{c}, u_{c}]$ where $_{c} = 0 = u_{c}$.³⁴ When either $_{c}$ or u_{c} equals zero for all c C, the market turns into the case studied in Section 4. Let $(_{c}, u_{c})_{c}$ c be the tolerance profile.

When the colleges hold a non-zero balance, then there may exist some colleges exporting (importing) more than they import (export). Then, we cannot represent all allocations by cycles. Therefore we need to consider chains in addition to the cycles. A which consider her acceptable, and c

Theorems 7 and 8 hold without any assumptions on preferences. Under a mild assumption on college preferences, we can show that 2S-TTTC is individually rational and it induces a dominant-strategy equilibrium for colleges' quota reporting game to certify all their students and report their true admission quota.

Although 2S-TTTC is defined in a static problem, we can easily extend it to the dynamic environment where the aggregate balance over years matters. In particular, for each period t and c C we can set counter b_c equal to c's aggregate balance in period t – 1 where the aggregate balance in period t – 1, is equal to the sum of balances between period 1 and t – 1. Moreover, the exogenous priority rule used in period t can be determined based on the aggregate balance colleges carry at the end of period t – 1 such that the highest priority can be given to the college with the highest aggregate balance and so on.

5 Temporary Worker Exchanges

Many organizations have temporary worker-exchange programs that can be modeled through our balanced two-sided matching framework. The first di erence between such programs and tuition exchange is that these exchanges are usually temporary. Each firm usually requires a set of specific skills, e.g., a mathematics teacher to replace their own mathematics teacher. Compatibility and ability to perform the task are the main preference criterion rather than a strict preference ranking. E.g., finding a good teacher with a specific degree is the first-order requirement, rather than finer details about the rankings of all good teachers.

The second di erence is that each position and each worker should be matched, unlike the tuition-exchange application. The workers are currently working for their home firms. Thus, the firms consider these workers necessarily acceptable. By contrast, in tuition exchange, colleges are not required to admit all the dependents of their employees. In temporary worker exchanges, a worker who does not want to go to a di erent firm necessarily stays employed in her home firm. We need to use a variant of the tuition-exchange model to facilitate balanced-e cient trade in such circumstances.

We can use the model introduced in Section 3 with slight changes. Since each firm accommodates its current workers, $q_c = |S_c|$ for each c Cfi g T (c) 9 1 9 9 5 5 # e (c) 9 1 9 9

Our paper, besides introducing a new applied problem and proposing a solution to it, has six main theoretical and conceptual contributions: We introduce a new two-sided matching model that builds on the two most commonly used matching models in the literature: discrete object allocation, including school (2012): "A Characterization of the Top Trading Cycles Mechanism in the School Choice Problem," working paper.

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Supplementary Material for "Two-Sided Matching via Balanced Exchange" by Umut Mert Dur and M. Utku Ünver

Appendix A On Current Practice of Tuition Exchange

In t s append x we analyze t e current practice of tu t on exc ange As t e centralized process s posely controlled once eac college sets ts end by the ty ad soon quota and end by e students are deter ned t end t end

su pt on states t at a better ad tted c ass s preferable as ong as t e net balance does not decrease ad ss on of unacceptable students deter orates t e rangings of uncon strained atc ngs regardless of t e r net balances and a college dee is the solution students unacceptable in tu t on exc ange. Assu pt on + introduces negative net balance averse preferences. In a results in t is section we we use Assu e provet s propos t on by construct ng an assoc ated Ga e ${\tt D}$ ap ey co ege ad ss ons an et n w c t e set of Ga e ${\tt D}$ ap ey stable atc ngs s

eore s λ and $\lambda \lambda$ do not conduct an equ br u ana vs s n a quota deter nat on ga e But t ey do point out t at n a frictioniess an et t e coneges t at will be device to ave a negative balance will be conservative and will decrease t e right by quotas for exports, will c will further deteriorate t e balances of ot er coneges

yp ca v no co ege fu v wt draws n pract ce ast ere soften a n u quota of part c pat on n p ace e con ecture t att s cou d be nst tuted because of t e reasons out ned above G ven t at cont nued e bers p s an attract ve bene t often t es s a er co eges w announce t att ey w port and export att s n u quota require ent and w cont nue to be a e ber of t e progra wt out fu v wt drawing fro t e syste

e concude t \mbox{at} under a new des g
n for tu \mbox{t} on exc \mbox{ange} t \mbox{ere} s
 $\mbox{ou}_{\bf d}$ be no roo

Acceptability: Ditudents w be assigned to nu co ege c_{\emptyset} w enever t ey point to t and ence t ey w never need to point to an unacceptable co ege. Hence a student cannot be assigned to an unacceptable co ege. Moreover, a student cannot point to a co ege t at considers er unacceptable erefore t e students ranged below in c cannot be assigned to c us f D C is acceptable.

Individual Rationality: Dence eac s is assigned to an option weak \checkmark better t an c_{\emptyset} s does not nd v dua \checkmark b c_{\emptyset} Dence a students n (c) are ranged above n c for eac c students w o are n t e cyc.es re oved n ound K of f D C w ere K s t e ast round of f D C ¹⁰ e w prove t at s ba anced e c ent n two parts

Part I: e rst prove t at cannot be Pareto do nated by anot er acceptable balanced atc ng If s (i) t en (s) C c_{\emptyset} s t e g est ranged opt on n s t at considers er acceptable at s no student s (i) can be assigned to a better college considering er acceptable. If t ere exists a latcing suct at s t en (s) considers s unacceptable at s cannot be Pareto do nated by anot er acceptable atc ng n w c at east one student n (i) s better o n

us ∮ D C s group strategy proof for students ■ e fo w ng e a s used n prov ng eore ⊭ Lemma 1 Proof of Theorem 4. e prove a stronger vers on of eore \leftarrow nder $\not D$ C suppose t at preference professare xed for conceges such that no concege reports an unacceptable student as acceptable in the temperature report. In the induced quota reporting gale under Assumption h this and on nant strategy equilibrium for a c C to cert for the temperature of temperature of temperature of the temperature of temperature of

en any acceptable ec an s w ass gn er to c_0 If $|(\lambda)| = 1$ or |(1)| = 1

one cyc

Step 1: Construct a preference pro $e \stackrel{\sim}{\succ} wt$ assoc ated ranging $\tilde{}$ as follows. Let student s is crangion y (s) as acceptable in $\tilde{}_s$ and $\stackrel{\sim}{\succeq}_j = \stackrel{\sim}{\succeq}_j$ for a $[(C) \setminus s]$. By the execution of the C algorithm f \mathfrak{D} C where see the constant f $\tilde{\mathfrak{D}}$ is strategy proof for students and acceptable $\swarrow [q \quad \stackrel{\sim}{\succeq}](s) = c_{\emptyset}$

en we c eq. w et er t e ass gn ents of students n $\overset{k-}{k'=}$ (') are t e sa e n $\swarrow [q \quad \tilde{\succeq}]$ and , If not t en for so e t ere ex sts a student \tilde{s} (") prefer r ng (\tilde{s}) to $\swarrow [q \quad \tilde{\succeq}](\tilde{s})$ and eac student n $\overset{k-}{k'=}$ (') gets t e sa e co ege n and $\Join [q \quad \tilde{\succeq}]$ en we repeat Etep λ by tag ng $\succeq := \tilde{\varsigma} s := \tilde{s}$ and $:= \tilde{,}$

s repet t on w end by t e n teness of rounds en a students n $\overset{k-}{k'=}$ (') get t e sa e co ege n e $\not D$ C outco e n $[q \quad \tilde{\succ}]$ and $\not [q \quad \tilde{\succ}]$ t en we proceed to \mathfrak{R} tep \not

Step 2: In Step λ we ave sown t at *s* prefers (*s*) to $\swarrow [q \stackrel{\sim}{\sim}](s) = c_{\emptyset}$ Suppose *c* st e o e co ege of *s* Stet a new e g b ty quota \tilde{c} equa to t e range of student *s* n *c* s nterna prorty order t at s $\tilde{c} = r_{c}(s)$ and et

co eges w c consider er acceptable and c_{\emptyset} If a student s assigned n t s round t en s e s ou d get t e sa e co ege n. Now consider students assigned n ound ' w en 1 A t e co eges t at a student prefers to er assign ent and consider er acceptable s ou d ave been re oved or beco e non porting n an ear er round e cannot a e t s student better o by assigning er to a co ege t at considers er $\begin{array}{cccc} {\tt D} nce \ we \ can \ run \ {\tt D} & C \ n \ t \ a \ v \ ass \ gn \ ng \ a \ ne \ g \ b \ e \ won \ ers \ to \ t \ er \ o \ e \ r \ s \\ t \ e \ proof \ of \ eore \ p \ es \ t \ e \ won \ ers \ trategy \ proofness \ of \ {\tt D} \ C \ \end{array}$

eore for un queness o ds wt a s g t c ange F rst note t at e proof of any Pareto e c ent student strategy proof and acceptable ec an s ass gns won ers to et ert er o e r sorbetter r st at consdert e acceptabe Inteunqueness part of t e proof e s proof adopted for $\mathbf{\hat{p}} = \mathbf{\hat{p}}$ C be ng t e on $\mathbf{\hat{y}}$ ec an s eore sat sfy ng Pareto e c ency student strategy proofness, acceptab $_{-}$ ty and respect for n terna prortes n
t e te porary won er exc ange ode w e updat ng won er
 s s preferences n \mathfrak{S} tep \mathbf{k} we do t as fo ows range (s) and er o e r as on \mathbf{v} acceptable r s n t e correct order of er true preferences. And t en at t e end of \mathfrak{S} tep \mathbf{k} s e w the assigned to er o e r under \swarrow \mathfrak{D} nce \varkappa respects nternation prorties and s acceptable student strategy proof and balanced e clent s w real real and e clent s w real and s w real and s real and n Step / en we reac Step / we w a ve a set of wor ers w o are assigned to t e r o e r s by \swarrow owever, a trad ng cyc.e between t e would prove tota, we fare w t out voatng ba $ancedness or feas b<math display="inline">_ty$

Immunity to Preference Manipulation by Colleges: eca.t at n any atc ng ba ancedness s sats ed and r s ter ad sson quotas Hence under Assu pt on f, r s are nd erent between any acceptable atc ng Dncet ef D C ec an s selects an acceptable atc ng w en r s report trut fully r s cannot be better o by an pulating ter preferences over te atc ngs and reporting quotas d erent fro ter true quotas

Stability: Cons der an arb trary an et $[q \gtrsim]$ Denote t e outco e of \mathcal{D} C by ecart at $q_c = |c|$ for a $c \in C$ a won ers cons der t er current r s acceptable a r s cons der t er current won ers acceptable and won ers w o are not cert ed re an at t er current r s Hence $|(c)| = q_c$ for a $c \in C$ D nce n a r s quotas are ed s nonwastefu. Note t at any utua dev at on of won er r par needs to end up w t a balanced atc ng D nce a e ployees n (c) are acceptable replacing one of t e e ployees n (c) w t anot er one n \land (c) cannot a c better o Hence cannot be blog ed by a won er r par

Appendix C Tuition-Exchange Programs

e rst exp a n w y tu t on exc ange progra s ex st n t e rst p ace because so e co eges c oose to subs d ze facu ty d rect y nstead of part c pat ng n tu t on exc ange progra s A t oug t s ay create ex b ty for t e students any d rect co pensat on

s taxable nco e w ereas a tuton exc ange sc o ars p s not 23 uton over exc ange s not considered to be an noo e transfer²⁴ Moreover, co eges ay not want to sw tc to suc d rect co pensat on progra s fro a cost sav ng perspect ve regard ess of t e tax bene t to t e facu ty e ber e present a s p e bag of t e enve ope ca cu at on to de onstrate t ese cost sav ngs ere are ore t an λ eyear co eges $n t \in \mathfrak{D}$ and at ost a f of t e ave e bers p to at east one tu t on exc angeDuppose n students are given tu t on exc ange ression scotars ps a year progra Instead f a co ege nances t e tu t on of a facu ty e bers c d t roug d rect cas co pensaton t en au tuton exc ange co eges w ave to pay n w ere st e average futut on cost of congeges However assung that average quates and sizes of congreges with and without turbon schonars in pare ties and equation of the set students of the set of the w attend a tuton exc ange co ege n return so t e co eges w on v get bag $\frac{nT}{2}$ e re a n ng $\frac{n}{2}$ s ots w te ed w t regu ar students egu ar students on average pay about a foft e tu ton t an s to ot er nanc a a d progra s For exa pe f f u t on D scount ng Dtudy of t e Nat ona Assoc at on of Correge and n vers ty Bus ness O cers report t at noo ng fres en pay on average 56% of fu $_{--}$ tu t on at a pr vate us t ey w n y pay $\frac{n\overline{1}}{1}$ to tu t on exc ange co eges As tu t on exc un vers ty c ange sc o ars ps const tute a very s a_{m} port on of co ege ad ss ons t s ca cu at on assu est at average tu ton pay ent woud not c ange by estabs ent of d rect cas co pensat on nstead of tu t on exc ange us as a result t e congress where m and m as a result t e congress where m as a result t e congress where m as a result t e congress where m are the result t e constant t e congress where m are the result t e congress wh about $\frac{n\overline{n}}{c}$ w c corresponds to one fourt of average fut t on per student uş t e tota per student sav ngs for t e facu ty e ber and t e co ege s ore t an a f of tu ton pay ent assu ng one trd of t $e\;d\;rect\;co\;$ pensat on s pad n $nco\;$ e tax at t e arg n by t e parent

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e poyees e g b e based on ts own rules Eac e ber college s required to accept at east t ree exclange students per year ere s not tat on on t e nu ber of exported students Eac cert ed student a so applies for ad iss on d rect v to t e e ber colleges of er c o ce. Cert ed students ust be ad itted by t e ost college n order to be considered for t e tu t on exclange sc o ars p. Eac year or e t an λ students bene t fron t is progra

Catholic College Cooperative Tuition Exchange (CCCTE) CCC E s co posed of e ber co eges Eac e ber co ege cert es ts e poyees as e g b e based on ts own rules Dudents ust be ad tted by t e ost co ege before applying for c ange of postons wit teac ers from countries including the Greece Finland. Net er ands India Mexico and the K Matching procedure is arranged by the Fulbrig tiprogratistic state and each conditional each school ust be approved before the latering are named.

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The Educator Exchange Program s organ zed by t e Canad an Educat on Exc ange Foundat on e progra neudes rec procanterprovincia and internationa exc anges e internationa destinations are Austra a Den and France Ger any Dwitzer and t e, K and Colorado t e, D

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poss b
 \P exc ange counterpart t en t e
y can exc ange t e r pos t ons before enter ng t e

The Erasmus Student Exchange Program s a ead ng exc ange progra between t e un vers t es n Europe Cose to for students ave part c pated s nce t started $n \downarrow$ e nu ber of students bene t ng fro t e progra s ncreas ng eac year $n \downarrow$ ore t an f students attended a co ege n anot er e ber country as

Appendix E Proofs of Appendix A

Proof of Proposition 3. e prove ex stence by s ow ng t at for any tu t on exc ange an et t ere ex sts an assoc ated co ege ad ss on an et and t e set of stable atc ngs are t e sa e under bot an ets inder Assu pt on we x at u t on exc ange an et $[q \gtrsim]$ Let E be t e set of e g b e students e rst introduce an assoc ated co ege ad ss ons an et e a Ga e D ap ey λ two s ded any to one atc ng an et $[C q \ s \ c]$ were t e set of students s. t e set of co eges s C t e quota vector of co eges for ad ss ons s q t e preference pro e of students over co eges s $s \ w \ c$ are a t e sa e ent t es ported fro t e tu t on exc ange an et and t e preference pro e of co eges over t e set of students s F na v we s ow t at f a atc ng s not stable for

3.b.i. If $\tilde{ ilde{c}}$ c

and et [($q'_c \ \hat{q}_{-c}$) ('_c ^_c) ≿] w ere '_c ^_c - 1 ■

Appendix F Structure of Stable Matchings

					а	b	С	d	е									
					3	5	2	2	2		•	-			,	-		
F a	۲h	1	Fa	F a	1	1	2	2	2	1	2	3	4	5	6	/	8	9
' a	۲ D	, (۶u	, e	4	I	3	3	3	h	h	0	0	h	0	0		0
1	3	6	7	9	5	6	4	4	8	0	0	u	C	0	a	C		C
2	Λ	5	Q		Q	2	Q	Q	7	c	c	c	a	a	b	a	c	
2	4	J	0			2			'	Ca	Ca	Ca	Ca	Ca	Ca	Ca	Ca	Ca
					7	7	7	5	5	- CØ	СØ	СØ	СØ	СØ	СØ	Cβ	СØ	CØ

rangengs of agents assoc ated with the repreferences over that a rungs are given as

Let o_e and o_a be t e vectors representing t e e g b ty and ad ss on counters of concepts respectively en we set $o_e = (2 \ 2 \ 2 \ 2 \ 1)$ and $o_a = (2 \ 2 \ 2 \ 1)$

Coverges a and c are resolved

Round 4: e on v cyc e for ed n ound $\underset{\mathbf{x}}{\mathbf{x}}$ s $(c_{\emptyset} \ \mathbf{7})$ erefore $\mathbf{7}$ s assigned to c_{\emptyset} G ven t at we ave a tr v a cyc e nc ud ng c_{\emptyset} we on v update o_{e}

are acceptable for congress e ranging associated with preference program is given as

Let ec an s \nearrow select t e sa e atc ng as \mathbf{D} C for eac an et except t e an et $[q = (1 \ 1 \ 1) = (1 \ 1 \ 1) \succeq]$ and for t s an et t ass gns 1 to c 2 to a and 3 to b s ec an s s balanced e c ent acceptable and respect ng nterna pror t es However t s not student strategy proof because w en 1 reports c unacceptable \swarrow w ass gn 1 to b

• A balanced-e cient, student-strategy-proof, but not acceptable mechanism that re-

represents t e co on tastes of students on c' X(s c') (0 1) s a so an d standard

w e sused as t e an or zonta ax s var ab e e vert ca ax s var ab es n top $\frac{1}{2}$ grap s de onstrate t e d erence of t e percentage of unass gned students between t e DA ec an s under t e two a ternat ve strateg es of t e co eges In eac row t e ist and rd grap s are for stra g tforward be av or of DA e, strategy i and t e nd and t grap s are for t e equiper u be av or of DA e, strategy i explained above and $\frac{1}{2}$ D

C:D C In botto +grap s t e vert ca axes de onstrate t e d erence between t e percentage of t e students preferr ng t e vers ons of D C and t e percentage of t e students preferr ng t e DA ec an s under two a ternat ve strateg es of t e co eges ³⁴ nder a scenar os w en we co pare t e percentage of students preferr ng t e ver s ons of D C and t e DA ec an s under two a ternat ve strateg es of t e co eges we observe t at D C and D C outperfor bot a ternat ve strateg c be av ors under DA For exa p e w en = 0.5 and = 0.5 for year v to erance eve 0 19.23% ore of a students e t e percentage of students w o prefer D C to DA nus t e percentage w o prefer DA to D C prefer D C outco e to DA strag tforward be av or outco e w e t s d erence ncreases to DA be avor scenar os On t e ot er and as , t e students preference correct on para eter ncreases $\neq D$ C s do nance easures d sp ay ost y a un oda pattern pea ng for oderate for any xed

and eac co ege as λ ava able seats D erent front e previous cases the number of students applying to be cert ed and vary and this selected from the network [6, 10] according to d unifor distribution. Preference professorial the students and the conjects are





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